



北京航空航天大学计算机学院

School of Computer Science and Engineering, Beihang University

多变量时序预测的公平性

领读人：寄家豪

北京航空航天大学计算机学院

先进计算机应用技术教育部工程研究中心



Learning Informative Representation for Fairness-aware Multivariate Time-series Forecasting: A Group-based Perspective

Hui He, Qi Zhang, Shoujin Wang, Kun Yi, Zhendong Niu, and Longbing Cao, *Senior Member, IEEE*



Hui He received the M.E. degree from University of Shanghai for Science and Technology, Shanghai, China in 2020. She is currently pursuing the Ph.D. degree at Institute of Engineering Medicine, Beijing Institute of Technology, Beijing, China. Her current research interests focus on multivariate time-series analysis and knowledge services.

机器学习中的公平性问题





- **Fairness** in [machine learning](#) refers to the various attempts at correcting [algorithmic bias](#) in automated decision processes based on machine learning models.
- Decisions made by computers after a machine-learning process may be considered **unfair** if they were based on [variables](#) considered **sensitive**.
- Examples of these kinds of variable include [gender](#), [ethnicity](#), [sexual orientation](#), [disability](#) and more.

一个模型对于不同的样本的拟合效果的一致程度。如果一个模型在某些样本上效果很好，另一些样本上效果不好，那么这个模型的公平性就比较差。



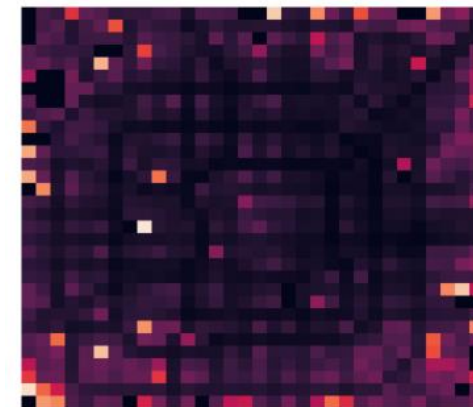
人脸识别



信用贷款



推荐系统



智能交通

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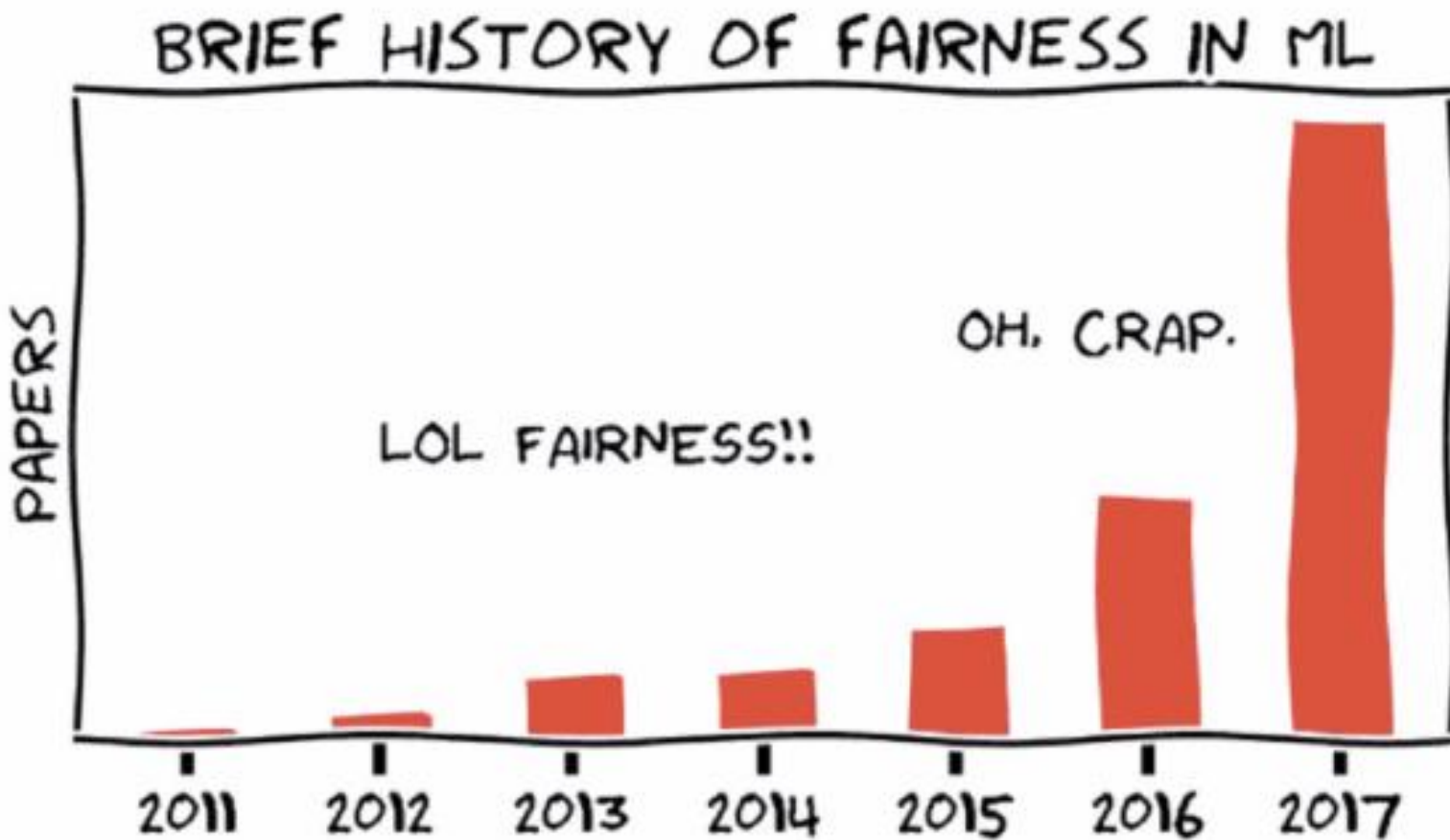


Fig1. The number of publications on fairness from 2011 to 2017

(Narayanan,
2018)

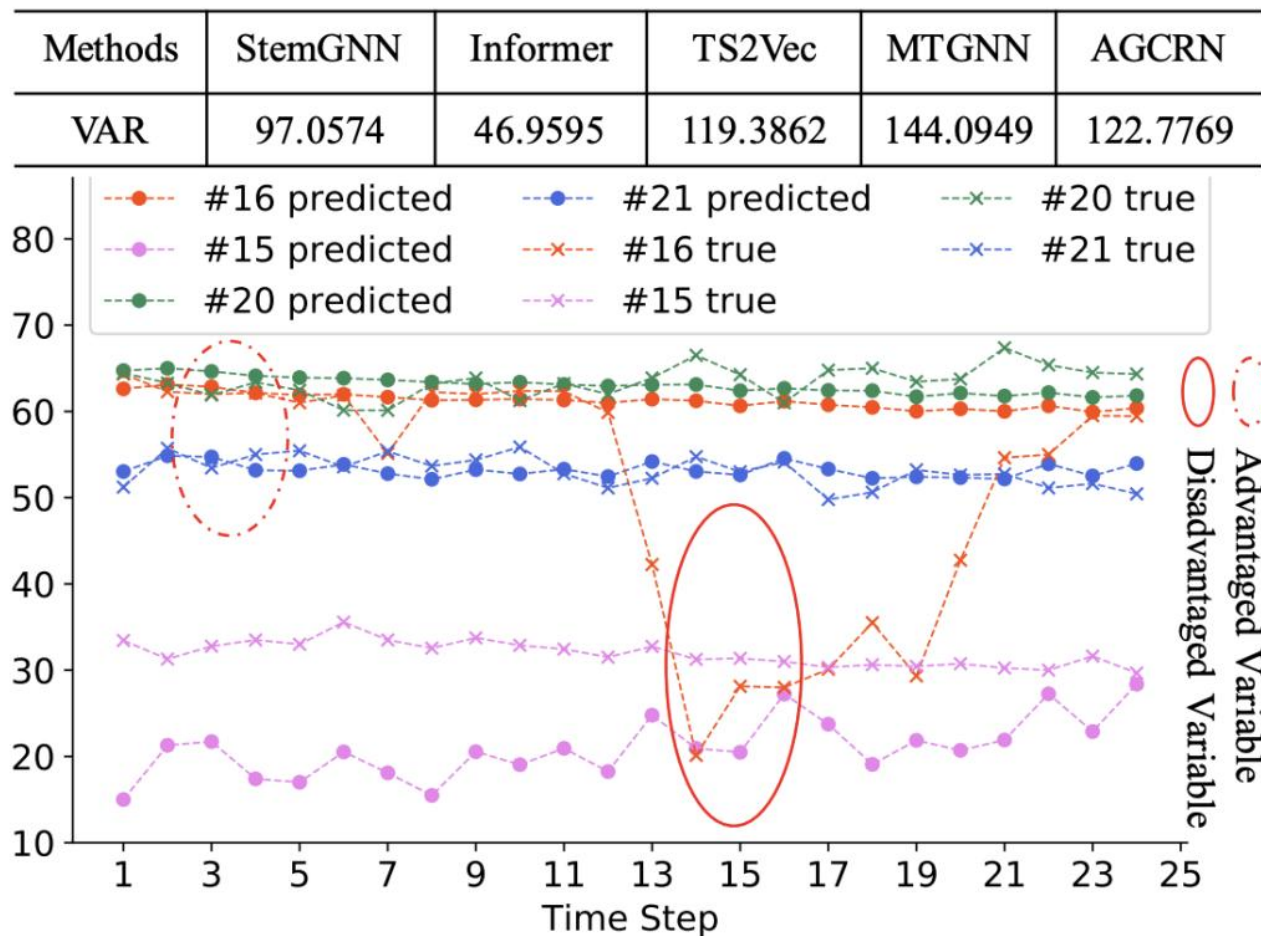
MTS预测中的公平性问题



MTS预测的公平性

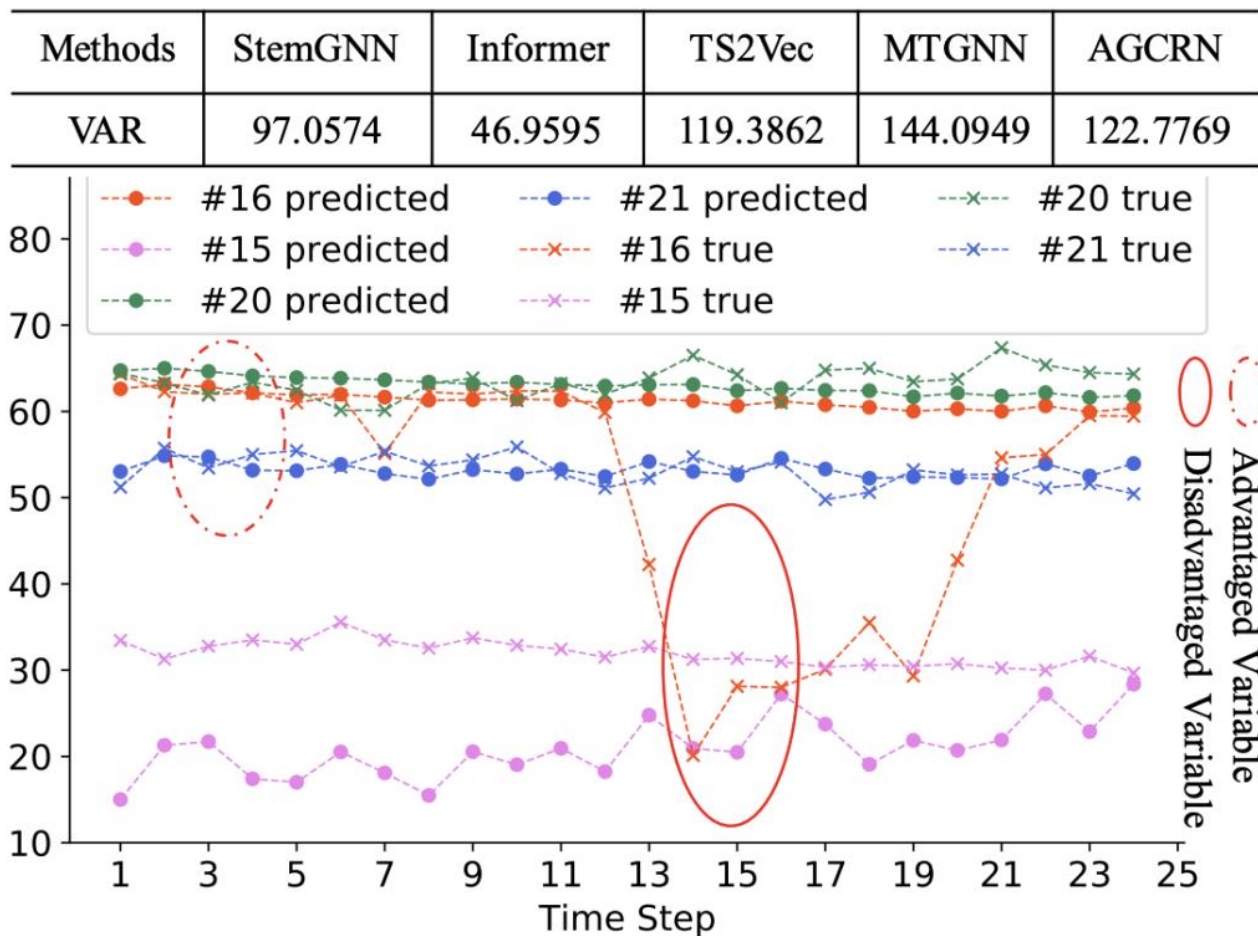


- 多源时序预测的公平性
 - 模型是否对各个变量的预测效果都比较好?



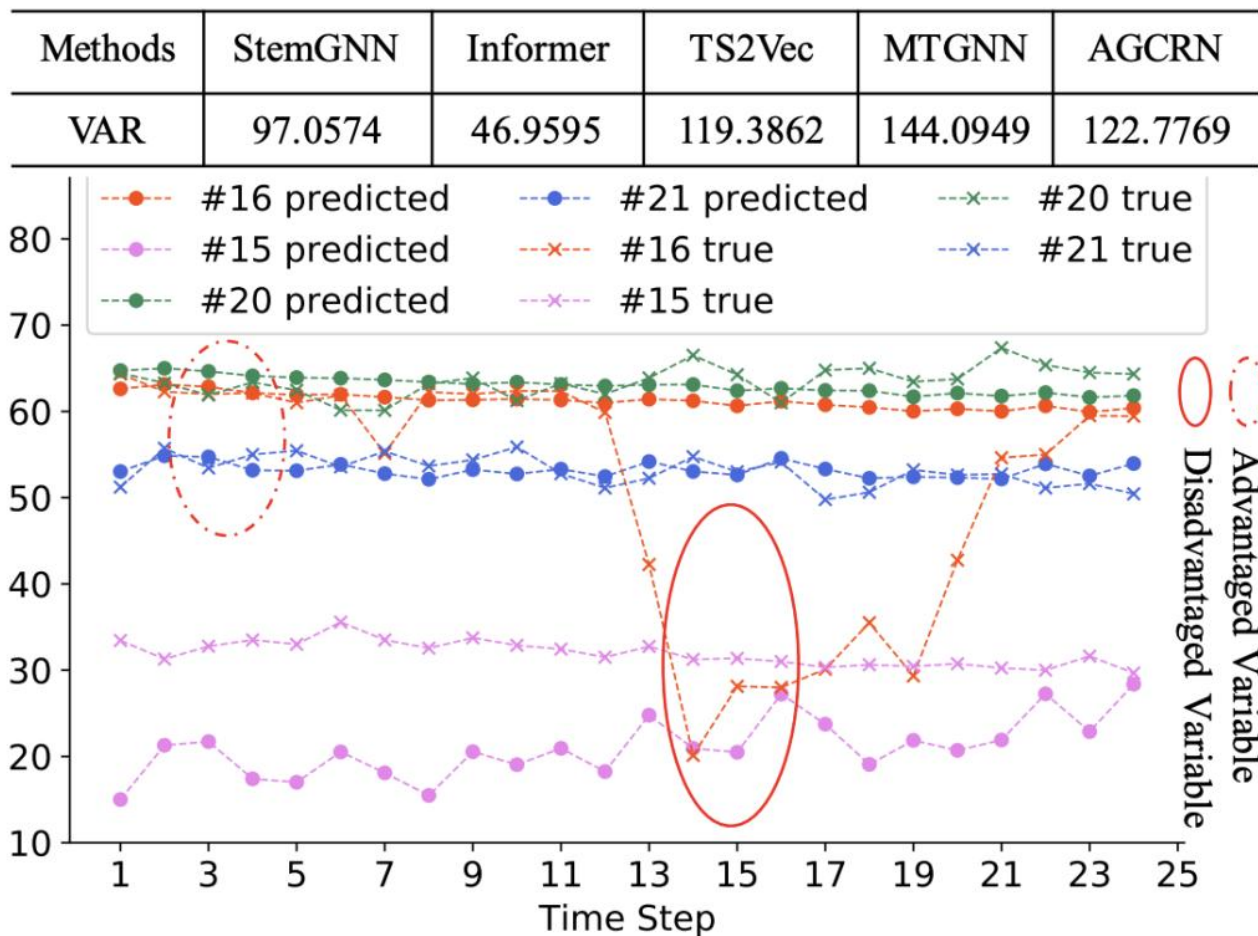


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 - 模型是否对各个变量的预测效果都比较好?
- 原因分析
 - 不同样本的特点不同, 模型在训练过程中可能被某些样本的特点主导





- 多源时序预测的公平性
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- 1、不同的变量，其序列pattern可能存在很大的差异
- 2、大部分序列都是平稳的，主导了模型的训练过程

解决方案

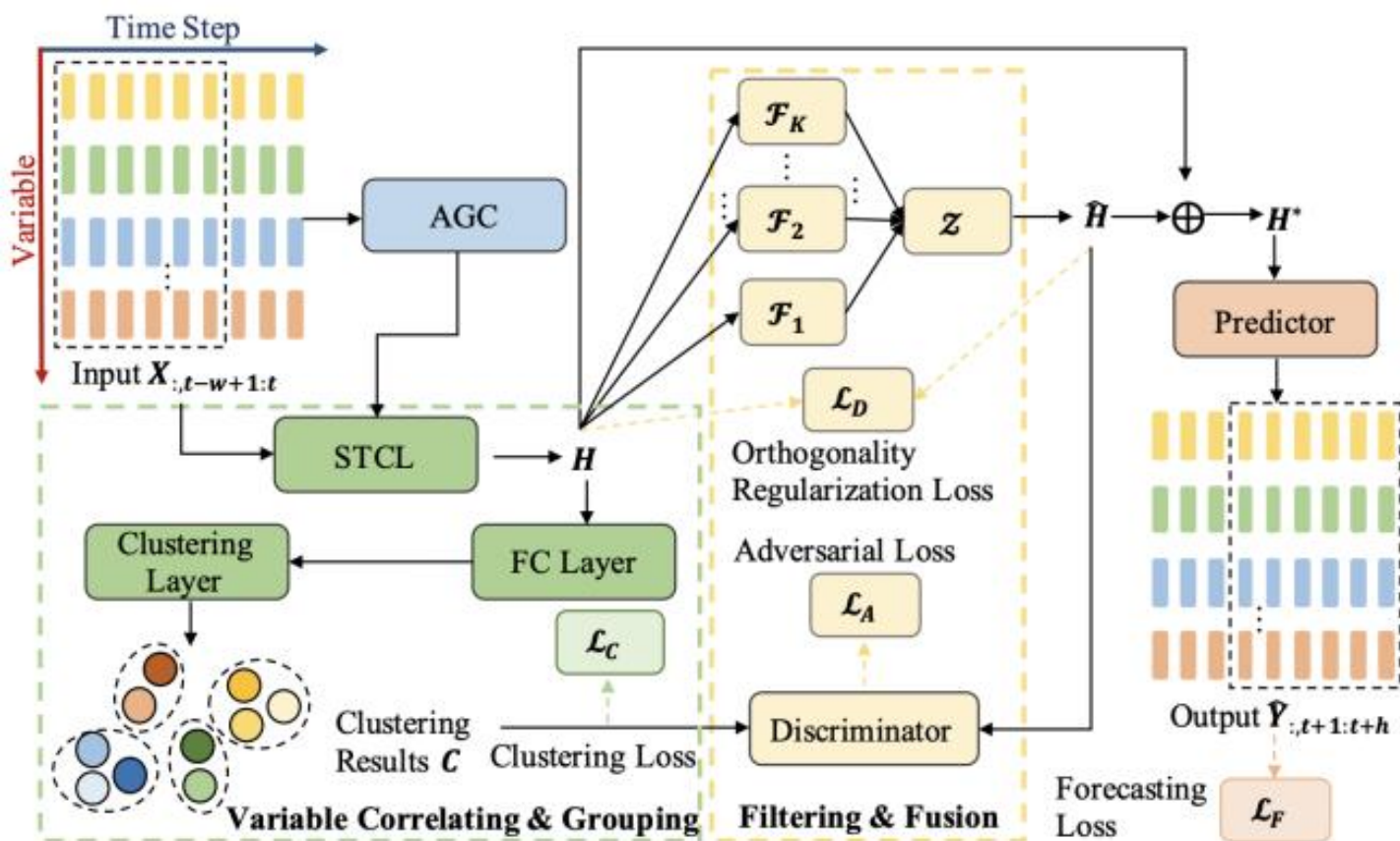




- 原因分析
 - 不同样本的特点不同，模型在训练过程中可能被某些样本的特点主导
- 解决思路
 - 将序列间的共性与特性分解开来，独立建模

Under the sliding forecasting setting with a fixed window size of $w \in \mathbb{N}^+$ and a sliding step of 1, we have the input, i.e., the observed values of all the N variables in w successive steps till the t^{th} time step, $\mathbf{X}_{:,t-w+1:t} = \{\mathbf{X}_{:,t-w+1}, \mathbf{X}_{:,t-w+2}, \dots, \mathbf{X}_{:,t}\} \in \mathbb{R}^{w \times N}$. We articulate the research problem of MTS forecasting on a graph $\mathcal{G} = (\mathcal{V}, \mathcal{E}, M)$ to emphasize the spatio-temporal correlations simultaneously. The set of nodes \mathcal{V} denotes input series $\mathbf{X}_{:,t-w+1:t}$, where $|\mathcal{V}| = N$ and each series/variable $\mathbf{X}_{i,:}$ corresponds to a node. \mathcal{E} represents the set of edges, and $M \in \mathbb{R}^{N \times N}$ is defined as the adjacent matrix. In addition, we evaluate the forecasting unfairness with the variance in forecasting errors of different variables, where the larger the variance is, the more unfair the forecasts are. Accordingly, the target is to accurately forecast based on the graph \mathcal{G} the future sequence of $h \in \mathbb{N}^+$ steps $\mathbf{Y}_{:,t+1:t+h} = \{\mathbf{Y}_{:,t+1}, \mathbf{Y}_{:,t+2}, \dots, \mathbf{Y}_{:,t+h}\}$ successive to the t^{th} time step through one forward procedure and guarantee a small forecasting error variance simultaneously.

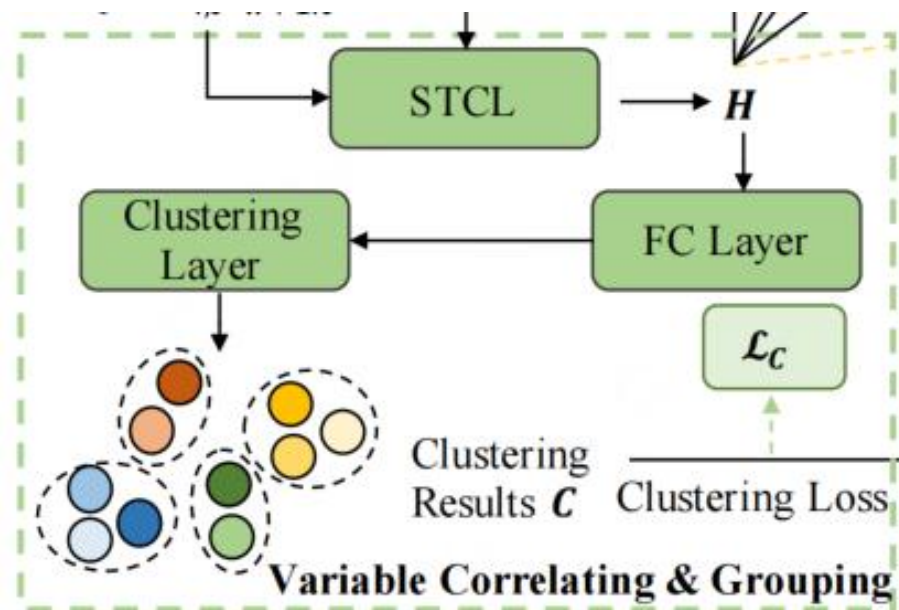
- 利用聚类的方法将多变量序列分组，得到不同组的表示
- 使用分解学习和对抗学习，从原始表示中剥离掉各个组特有的信息，得到公共的信息
- 通过前两步实现公共信息和特有信息的剥离，再基于这两个部分信息进行最终预测



- **K-Means**聚类的优化目标为：
 - 最小化样本到样本中心的距离和
 - 其可以通过**Spectral relaxation**转化为以下损失函数[1]

$$\mathcal{L}_C = \text{Tr}(\mathbf{H}^T \mathbf{H}) - \text{Tr}(\mathbf{F}^T \mathbf{H}^T \mathbf{H} \mathbf{F}) \quad s.t. \mathbf{F}^T \mathbf{F} = \mathbf{I}$$

- 其中，**F**是**H**的前**k**个奇异向量
- 前提：**H**是固定的
- **EM**迭代优化：
 - 固定**H**，**SVD**求**F**
 - 固定**F**，训练几轮**H**



模型细节2：分解学习与对抗学习



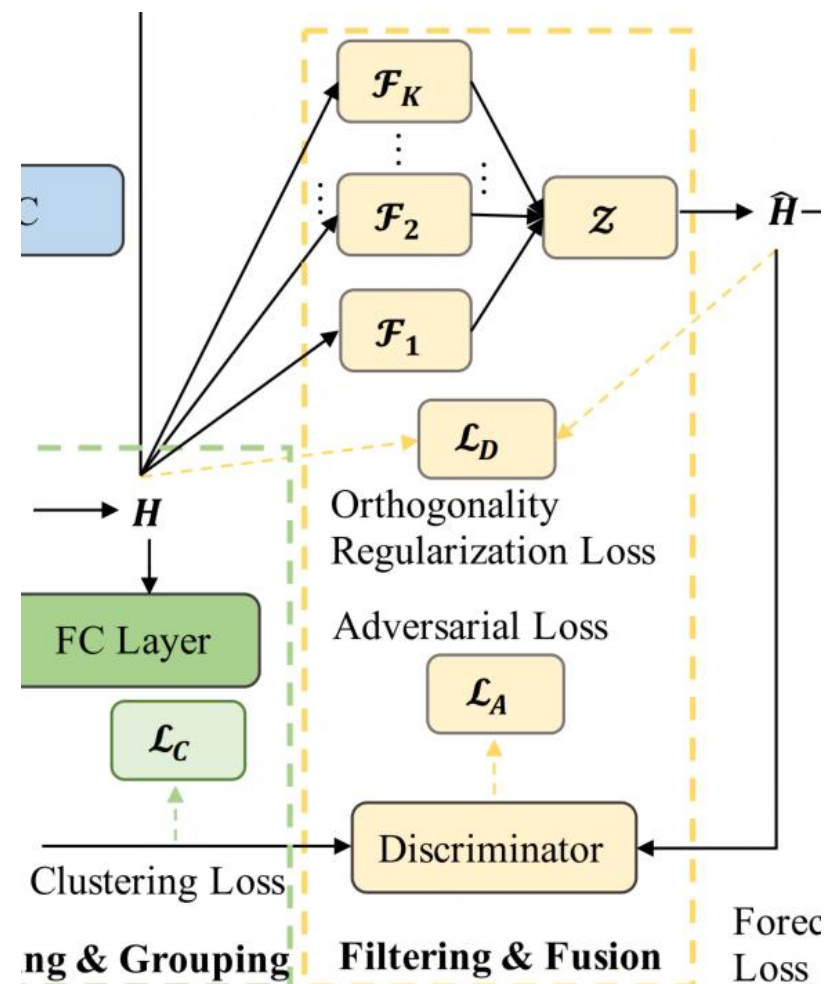
- 分解学习：过滤掉group相关的信息

$$\widehat{H} = Z(\mathcal{F}_1(H), \mathcal{F}_2(H), \dots, \mathcal{F}_K(H))$$

- F_k 是第k个group对应的过滤器 (FC实现)
- Z 是合并函数，如取平均

- 对抗学习： $\mathcal{L}_A = \frac{1}{N} \sum_{i=0}^{N-1} \|\widehat{H}_i - C_i\|_2^2$ **F、Z函数**

- 正则项：推广group相关和group无关表征的距离 $\mathcal{L}_D = \frac{1}{N} \sum_{i=0}^{N-1} \left| \frac{\widehat{H}_i \cdot H_i}{\|\widehat{H}_i\| \cdot \|H_i\|} \right|$



模型细节3：序列表示学习



- 自适应图构造**AGC**:

$$\tilde{M} = \delta(\text{ReLU}(\mathbf{E}_M \cdot \mathbf{E}_M^T))$$

- 时空关系学习**STCL**:

- 在**GRU**基础上，每个单元的计算引入了**GCN**模块

- 类似于**DCRNN** (Li et al,

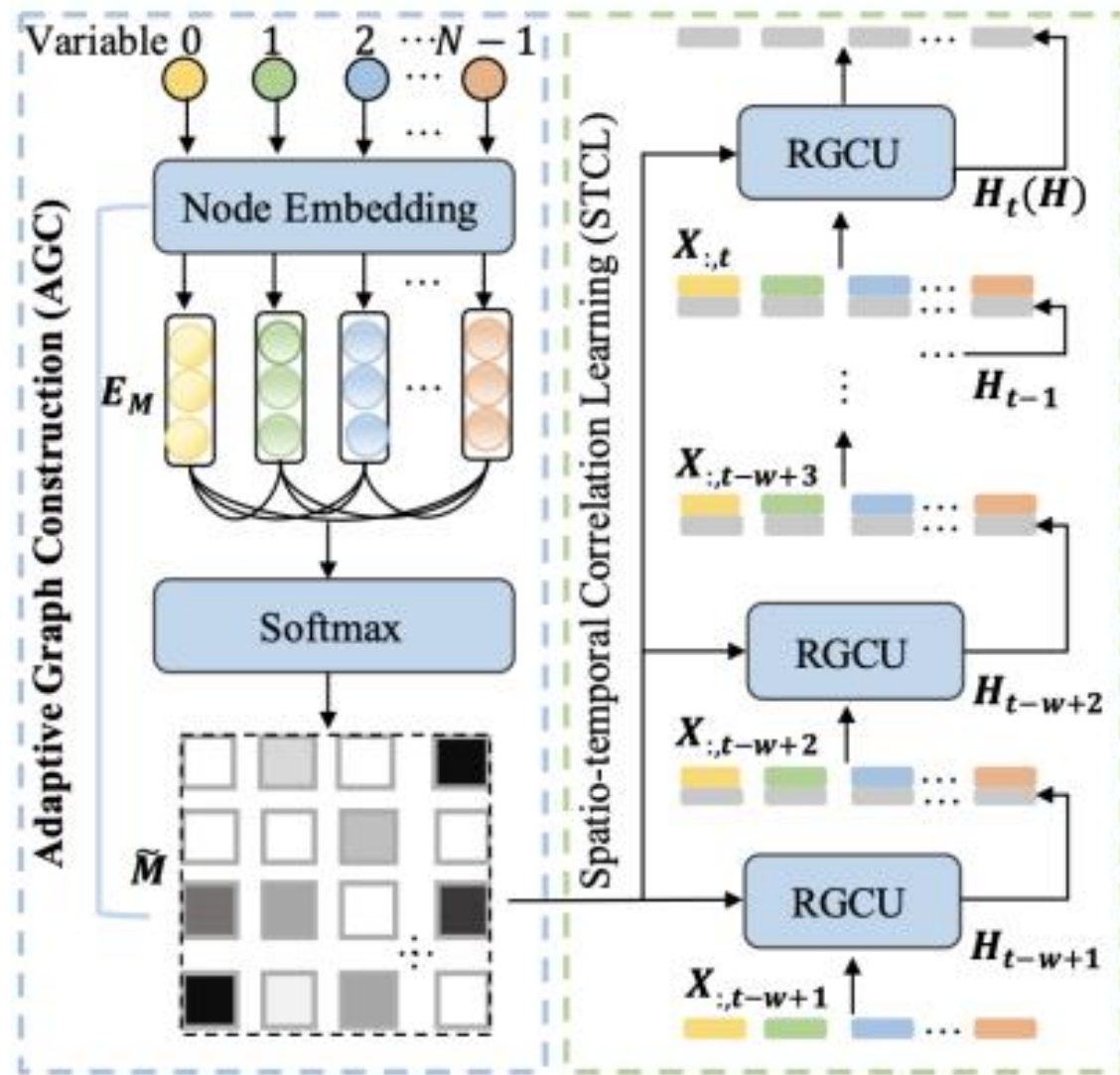
$$\tilde{M} = \delta(\text{ReLU}(\mathbf{E}_M \cdot \mathbf{E}_M^T))$$

$$\mathbf{r}_t = \sigma(\tilde{M}[\mathbf{X}_{:,t} || \mathbf{H}_{t-1}] \mathbf{W}_r + \mathbf{b}_r)$$

$$\mathbf{u}_t = \sigma(\tilde{M}[\mathbf{X}_{:,t} || \mathbf{H}_{t-1}] \mathbf{W}_u + \mathbf{b}_u)$$

$$\mathbf{c}_t = \theta(\tilde{M}[\mathbf{X}_{:,t} || \mathbf{r} \odot \mathbf{H}_{t-1}] \mathbf{W}_c + \mathbf{b}_c)$$

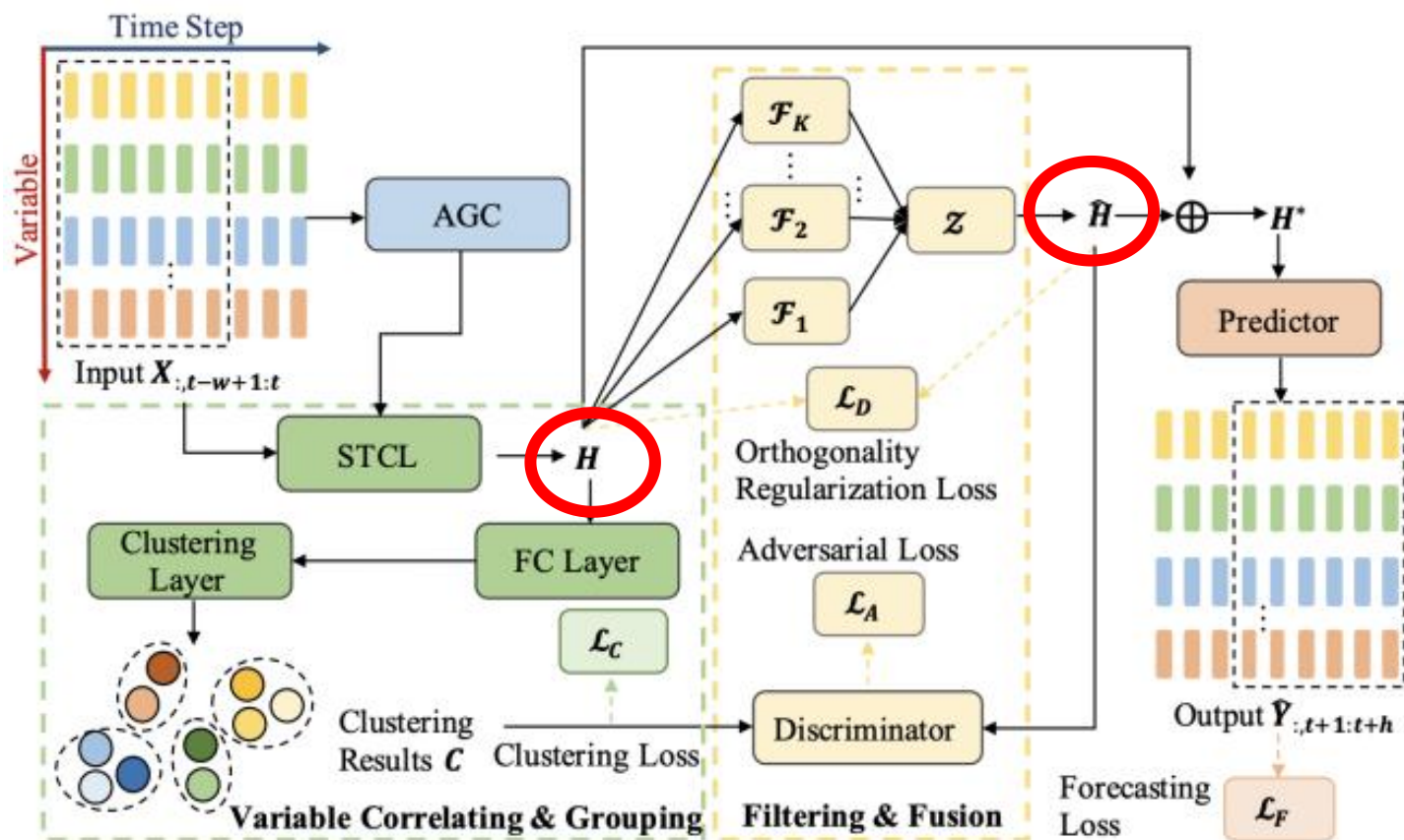
$$\mathbf{H}_t = \mathbf{u} \odot \mathbf{H}_{t-1} + (1 - \mathbf{u}) \odot \mathbf{c}_t$$



模型细节4：最终预测



- 联合group相关和group无关的表征做预测





Algorithm 1 Adversarial Training for *FairFor*

Require: Hidden state \mathbf{H} , group results \mathbf{C} , network \mathcal{R} , filter and fusion functions $\mathcal{F}, \mathcal{Z} \subseteq \mathcal{R}$, discriminator \mathcal{D} and cluster number K

- 1: Orthogonal initialize cluster indicator matrix \mathbf{F}
 - 2: **for** each training iteration i **do**
 - 3: $\widehat{\mathbf{H}} \leftarrow \mathcal{Z}(\{\mathcal{F}_k\}_{k \in [K]}(\mathbf{H}))$ by Eq. (10)
 - 4: $\mathbf{H}^* \leftarrow \mathbf{H} + \widehat{\mathbf{H}}$
 - 5: Optimize \mathcal{L} w.r.t $\mathbf{H}, \widehat{\mathbf{H}}, \mathbf{H}^*, \mathbf{C}, \mathcal{R}$ with \mathcal{D} being fixed
 - 6: **if** $i \% 3 == 0$ **then**
 - 7: Update \mathbf{F} by computing K -truncated SVD of \mathbf{H}
 - 8: **end if**
 - 9: $\mathcal{L}_A \leftarrow \mathbb{E}[\|\widehat{\mathbf{H}} - \mathbf{C}\|_2^2]$ by Eq. (11)
 - 10: Optimize \mathcal{L}_A w.r.t $\widehat{\mathbf{H}}, \mathbf{C}, \mathcal{D}$ with $\mathcal{R}, \mathbf{H}, \mathbf{H}^*$ fixed
 - 11: **end for**
-

实验结果





| Tasks | #Time Step | #Variable | Interval | Start Time |
|--------------|------------|-----------|----------|------------|
| Traffic | 10,392 | 963 | 1hour | 1/1/2008 |
| PeMSD7(M) | 11,232 | 228 | 5min | 7/1/2016 |
| Solar-Energy | 52,560 | 137 | 10min | 1/1/2016 |
| ECG5000 | 5,000 | 140 | — | — |

PeMSD7(M) [1] records the traffic flow data of the detectors in California. It includes 228 variables and 11,232 time steps at a 5-minute interval;

Solar-Energy [2] is collected from National Renewable Energy Laboratory (NREL) and records the solar power production in 2006. It includes 137 variables and 52,560 time steps at a 10-minute interval;

Traffic [3] is originally collected from the California Department of Transportation and describes the occupancy rate of different lanes in San Francisco highway. It contains 963 variables and 10,560 time steps with a 10-minute interval, where each observation is between 0 and 1;

ECG5000 [4] records 5,000 heartbeats randomly selected from a 20-hour long ECG downloaded from Physionet. It contains 140 variables and 5,000 time steps.

LSTNet [7]: integrates RNNs and CNNs to capture the short- and long-term temporal patterns respectively;

TPA-LSTM [8]: embeds temporal pattern attention into RNNs to discover both relevant time series and time steps;

TS2Vec [54]: is a dilated CNN based universal framework to capture multi-scale contextual information in MTSs;

Informer [9]: is a Transformer-based model with *ProbSparse* self-attention mechanism and generative style decoder to predict long time series at one forward step;

Pyraformer [10]: is a Transformer-based model to simultaneously extract multiple ranges of temporal dependencies via the compact multi-resolution operation;

MTGNN [46]: combines graph learning, graph convolution and temporal convolution together to learn the spatial-temporal correlations without pre-defined graph structure;

StemGNN [12]: uses a GCN-based spectral network that can capture inter-series dependencies and temporal correlations jointly in the spectral domain;

AGCRN [4]: employs GCNs embedded with an adaptive node-specific pattern learning module to capture fine-grained inter-series relationships and uses RNNs to capture temporal patterns.



| Dataset | Metric | LSTNet | TPA-LSTM | TS2Vec | Informer |
|--------------|--------|---------|----------|---------|----------------|
| PeMSD7(M) | VAR | 23.6003 | 42.2336 | 28.4647 | 28.1218 |
| Solar-Energy | | 5.6880 | 10.1448 | 5.2330 | <u>5.2096</u> |
| Traffic | | 9.51e-4 | 8.07e-4 | 5.30e-4 | <u>4.27e-4</u> |
| ECG5000 | | 0.5668 | 0.2577 | 0.2360 | 0.2257 |

| Pyraformer | MTGNN | StemGNN | AGCRN | <i>FairFor</i> |
|------------|---------|---------------|----------------|----------------|
| 48.4494 | 42.7716 | 26.5534 | <u>22.7220</u> | 20.3152 |
| 10.6149 | 9.7419 | 5.7216 | 5.6543 | 5.1188 |
| 7.63e-4 | 6.43e-4 | 6.71e-4 | 5.59e-4 | 4.17e-4 |
| 0.2618 | 0.2255 | <u>0.1774</u> | 0.2467 | 0.1732 |

所有数据集预测公平性均有提升: **Improvement:**

10.59%/1.74%/2.34%/2.37%

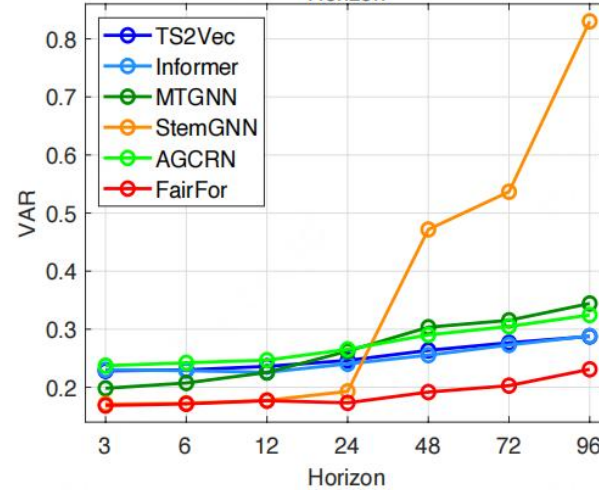
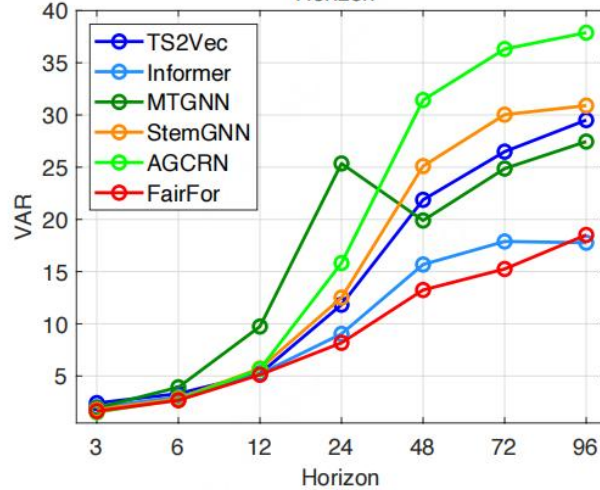
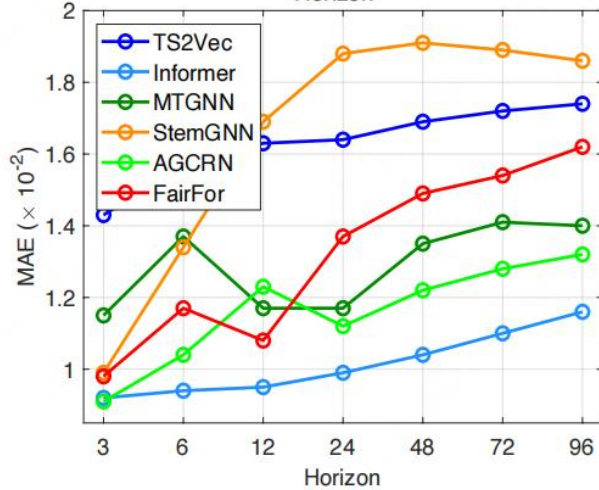
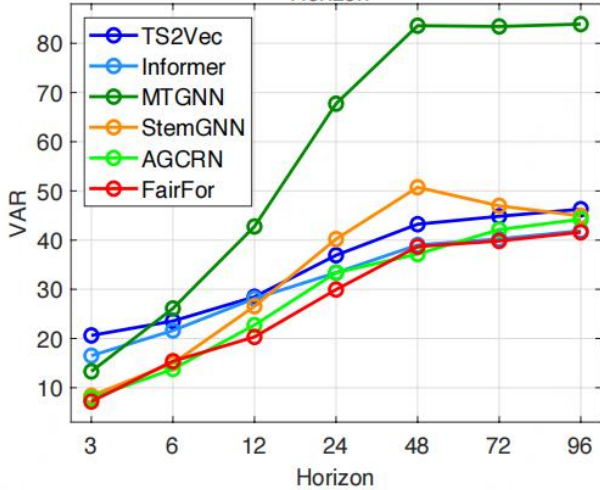
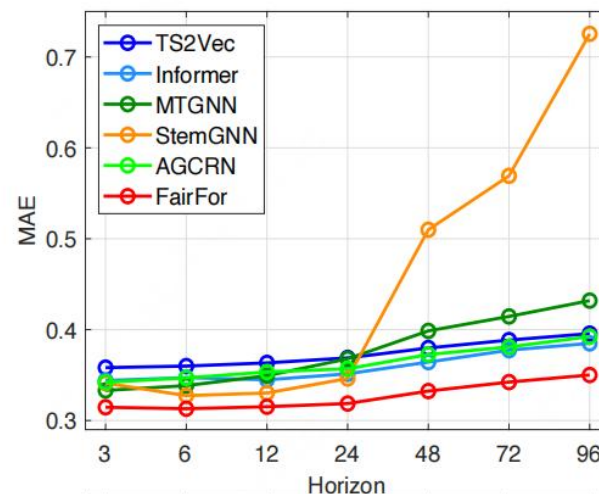
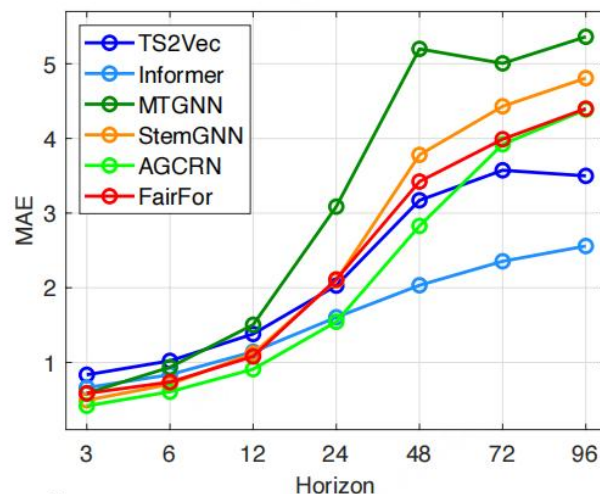
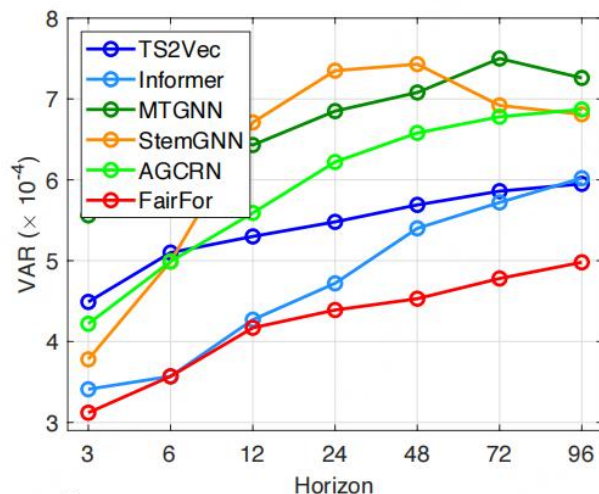
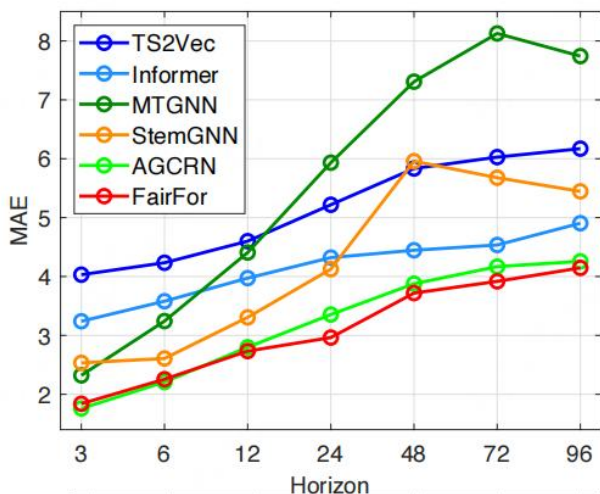
预测精度结果



- 公平性可以提升准确率（一定程度上）

| Dataset | Metric | LSTNet | TPA-LSTM | TS2Vec | Informer | Pyraformer | MTGNN | StemGNN | AGCRN | <i>FairFor</i> |
|--------------|--------|--------|----------|--------|---------------|---------------|--------|---------------|---------------|----------------|
| PeMSD7(M) | MAE | 3.2004 | 4.7573 | 4.6001 | 3.9728 | 4.2925 | 4.4072 | 3.3064 | <u>2.7983</u> | 2.7336 |
| | RMSE | 5.6566 | 7.8292 | 7.0445 | 6.6654 | 8.1646 | 7.5602 | 5.7927 | <u>5.4950</u> | 5.2798 |
| | MAPE | 0.0870 | 0.1932 | 0.1117 | 0.0957 | 0.1067 | 0.1127 | 0.0817 | <u>0.0694</u> | 0.0678 |
| Solar-Energy | MAE | 1.3030 | 2.0399 | 1.3810 | 1.1426 | 2.2316 | 1.5043 | 1.1205 | 0.9090 | <u>1.0807</u> |
| | RMSE | 2.7057 | 3.1682 | 2.6721 | 2.5702 | 3.9558 | 2.7029 | 2.6720 | 2.5457 | <u>2.5608</u> |
| | MAPE | 3.4220 | 3.4175 | 3.3694 | 3.3826 | 3.4080 | 3.3727 | 3.4096 | 3.2905 | <u>3.3584</u> |
| Traffic | MAE | 0.0220 | 0.0158 | 0.0163 | 0.0095 | 0.0445 | 0.0117 | 0.0169 | 0.0123 | <u>0.0108</u> |
| | RMSE | 0.0374 | 0.0317 | 0.0282 | 0.0215 | 0.0523 | 0.0279 | 0.0310 | 0.0260 | <u>0.0240</u> |
| | MAPE | 0.7736 | 0.4924 | 0.5630 | 0.2482 | 2.2674 | 0.3429 | 0.4768 | 0.2676 | <u>0.2669</u> |
| ECG5000 | MAE | 0.4978 | 0.4268 | 0.3634 | 0.3448 | <u>0.3287</u> | 0.3493 | 0.3303 | 0.3534 | 0.3152 |
| | RMSE | 0.9022 | 0.6874 | 0.6067 | 0.5921 | 0.6110 | 0.5769 | <u>0.5352</u> | 0.6096 | 0.5207 |
| | MAPE | 0.9334 | 0.9561 | 0.9664 | 0.9481 | 1.0132 | 0.951 | <u>0.9176</u> | 0.9854 | 0.8931 |

预测精度结果



(a) PeMSD7(M)

(b) Solar-Energy

(c) Traffic

(d) ECG5000

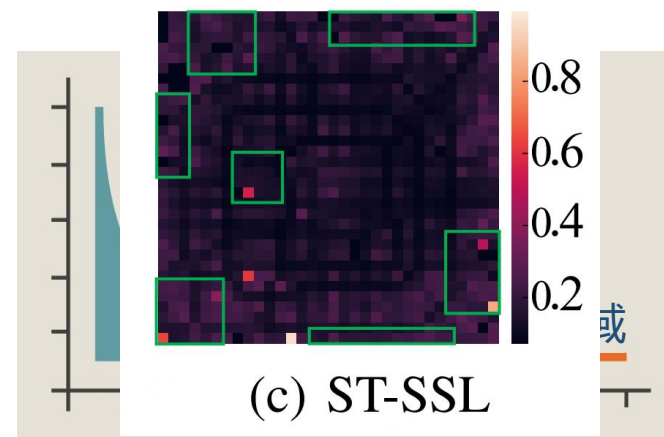
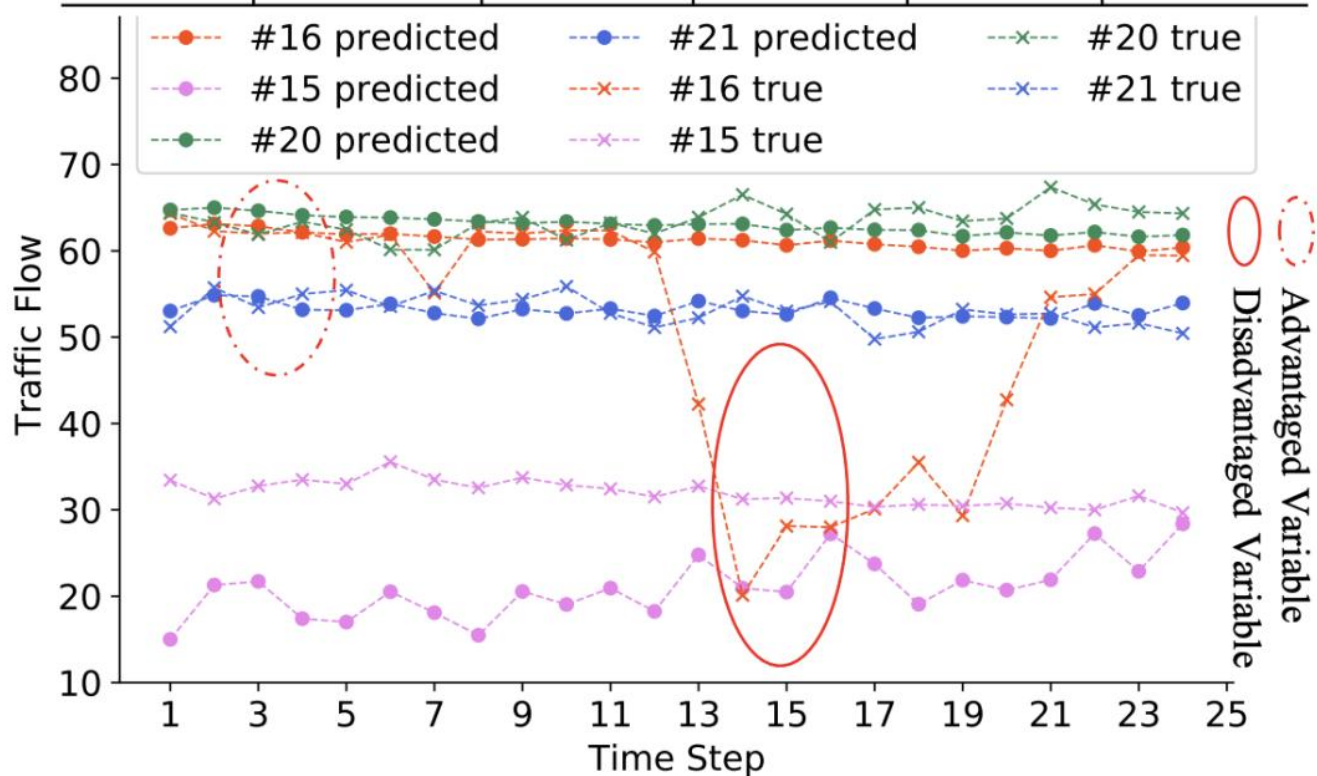


- 准确率是讨论公平性的基本，没有准确率讨论公平性的意义不大！

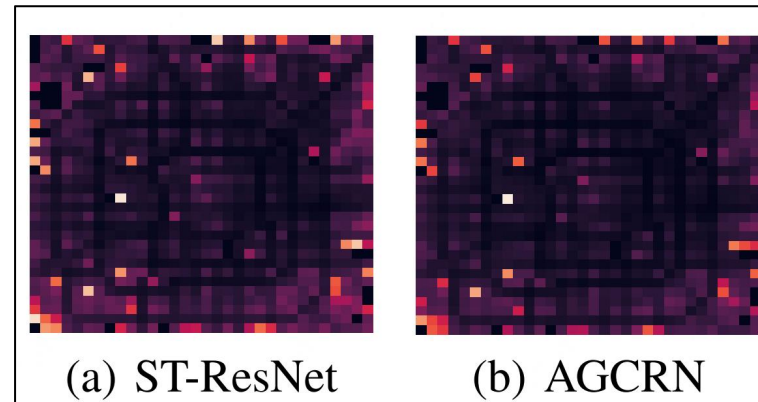
| Models | PeMSD7(M) | | | Solar-Energy | | | Traffic | | | ECG5000 | | |
|----------------|---------------|---------------|----------------|---------------|---------------|---------------|---------------|---------------|----------------|---------------|---------------|---------------|
| | MAE | MAPE | VAR | MAE | MAPE | VAR | MAE | MAPE | VAR | MAE | MAPE | VAR |
| w/o STCL+AGC | 4.2412 | 0.1018 | 30.2543 | 1.5797 | 3.4438 | 6.1499 | 0.0164 | 0.4758 | 5.93e-4 | 0.4500 | 0.9024 | 1.0522 |
| w/o ALD | 2.8889 | 0.0689 | 20.0300 | 1.3456 | 3.4157 | 5.3100 | 0.0142 | 0.3541 | 4.38e-4 | 0.3159 | 0.8982 | 0.1744 |
| w/o CL | 2.8522 | 0.0689 | 20.3052 | 1.2181 | 3.3994 | 5.2194 | 0.0145 | 0.3471 | 4.47e-4 | 0.3161 | 0.8976 | 0.1749 |
| w/o ORL | 2.8497 | 0.0690 | 20.3152 | 1.1736 | 3.3865 | 5.2112 | 0.0138 | 0.3784 | 4.56e-4 | 0.3159 | 0.8960 | 0.1747 |
| <i>FairFor</i> | 2.7983 | 0.0678 | 19.9953 | 1.0807 | 3.3826 | 5.1188 | 0.0123 | 0.3429 | 4.27e-4 | 0.3152 | 0.8931 | 0.1732 |

• 公平性 (Fairness) 与鲁棒性 (Robustness) 的区别与联系

| Methods | StemGNN | Informer | TS2Vec | MTGNN | AGCRN |
|---------|---------|----------|----------|----------|----------|
| VAR | 97.0574 | 46.9595 | 119.3862 | 144.0949 | 122.7769 |



长尾分布导致模型偏向热门区域





- 时空+公平性研究是一片蓝海，大家快来一起探索！
- 公平性可以一定程度上提升准确率
- 准确率是讨论公平性的基本
- 通过拆分不变和变化的表征可以提升公平性



感谢各位!

